



**Pacific  
Northwest**  
NATIONAL LABORATORY

# Harmonic Enhanced Load Modeling and Data Generation

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U.S. DEPARTMENT OF  
**ENERGY** **BATTELLE**

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# Acknowledgment

- **Sponsor:**
  - *Sensor Technologies and Data Analytics Program* (US DOE OE)
  - **Title:** Continual **Harmonic-Enhanced Load Modeling (HELM)** project
  - **Project Period:** FY21-FY22 (ongoing)
- **PNNL Team**
  - **Jim Ogle, Don Hammerstrom, Andy Reiman, Ankit Singhal, Dexin Wang, Tim Yin, Bhaskar Mitra, April Sun**



U.S. DEPARTMENT OF  
**ENERGY**

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# What We Cover Today

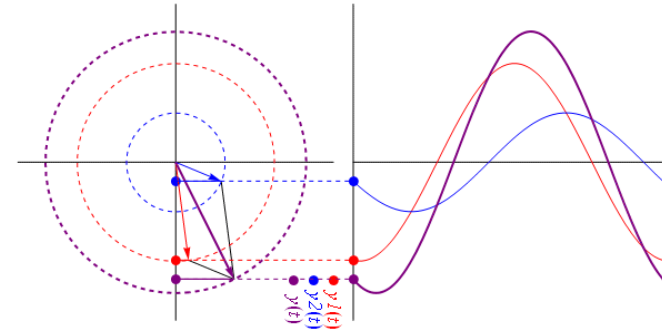
- **Harmonic Load Models**
  - Harmonics in loads
  - Impact of harmonics
  - Gaps in existing models
- The HELM approach
- Current results and plan

# Harmonics: Concept

- Power system is designed to operate at frequency of 60Hz (fundamental).
- Harmonics are the integer multiples of the fundamental (*typically, only odd*)

$$s(t) = \sum_{k=-\infty}^{+\infty} S[k] \cdot (\cos(k\omega t) + j \sin(k\omega t))$$

*Fourier series establishes the equivalence between time-domain and frequency domain, for periodic waveforms*

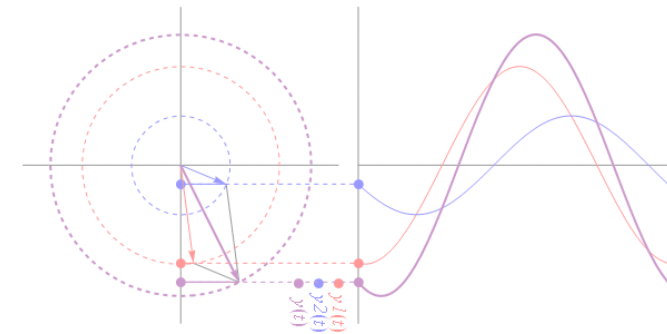


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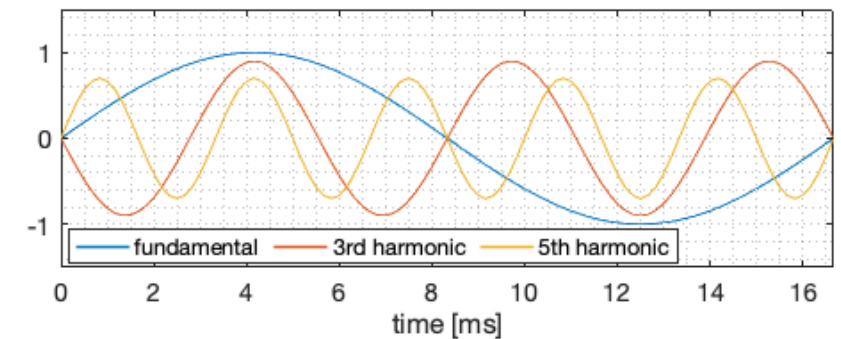
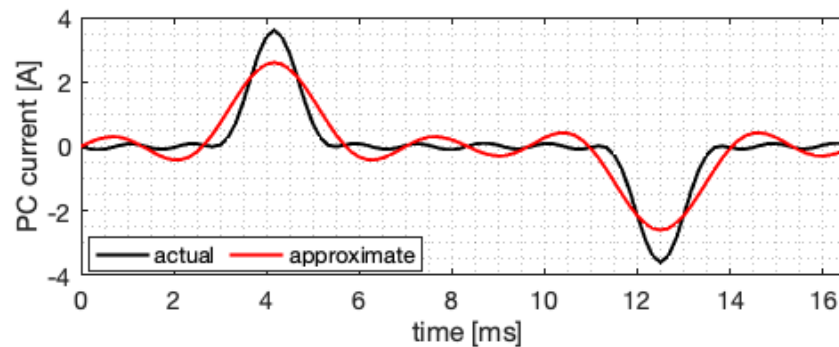
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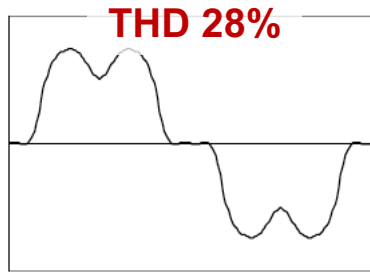


**Example: current waveform of a desktop computer**

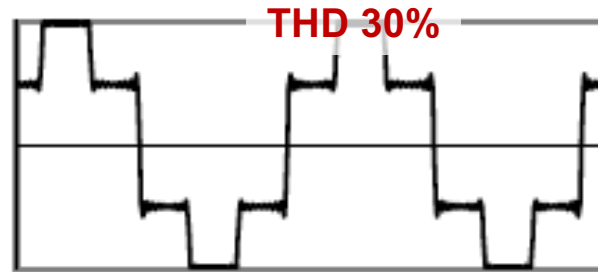


# Harmonics: Sources

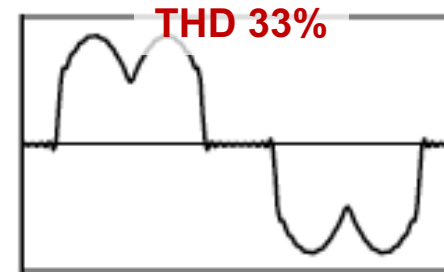
- Major source of harmonics are different nonlinear loads and devices
- Power-electronic loads:



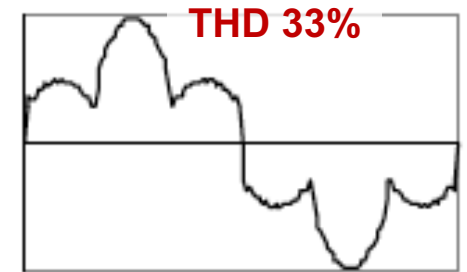
*Adjustable Speed Drives (ASDs)*



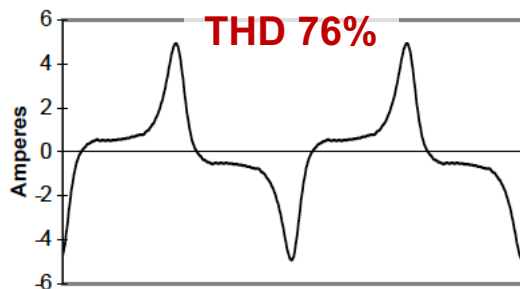
*Line Commutated Converter*



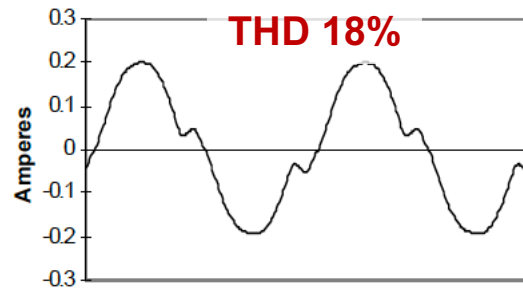
*Voltage Source Converters (high power)*



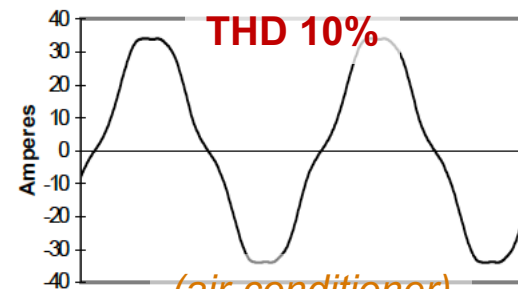
- Other nonlinear loads:



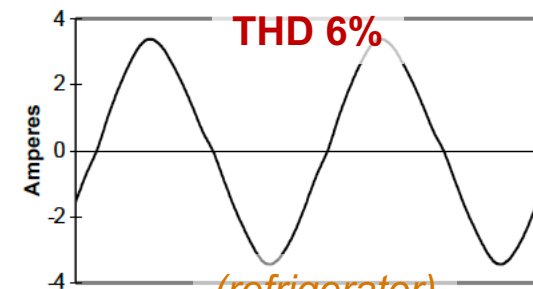
*Transformer*



*Fluorescent lamp*

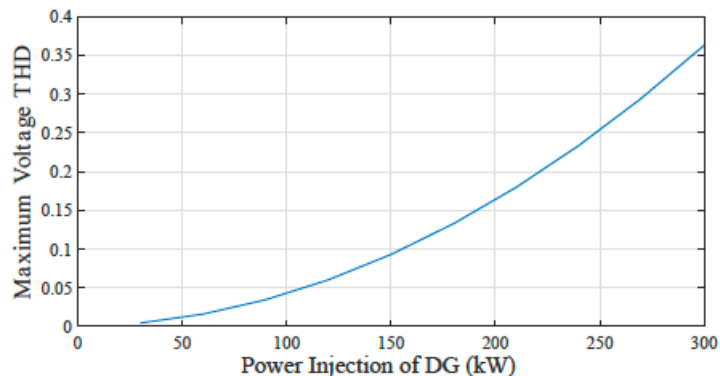


*Induction motor loads*



# Effects of Harmonics in Grid


- Overheated transformers (*current harmonics*) *17% loss in transformer kVA rating due to eddy current loss factor of 0.1*
- Harmonics lead to inaccuracies in ZIP models *63% error in ZIP model at 5% THD in voltage [McLorn et al, 2017]*
- Blowing of capacitor fuses (voltage harmonics) *40% increase in capacitor RMS current due to 10% THD in voltage*
- Distributed generation (DG) increases harmonics



*Tian et al, 2017, demonstrated the impact of growing penetration of power-electronic distributed generation on the THD of the network voltages*

# Gaps in Existing Load Models

- **Conventional ZIP**: constant impedance (Z), current (I), and power (P), evaluated only at the fundamental frequency

$$\begin{aligned} S &\approx S_1 && \text{RMS of only the} \\ &= V_1 \cdot I_1 && \text{fundamental components} \\ &= a V_1^2 + b V_1 + c \end{aligned}$$




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*RMS of only the fundamental components*

- **Adjusted ZIP**: small multiplying factor to account for current harmonics
  - **No consideration of voltage harmonics**
  - Only cumulative, not individual harmonics

$$\begin{aligned} S &\approx V_1 \cdot (I_1 + I_H) \\ &= S_1 (1 + \alpha) \end{aligned}$$

*allow a small correction factor, accounting for harmonics in current*

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 &&& \text{harmonics in current}
 \end{aligned}$$

- **Norton Model:** linear relationship between corresponding harmonic components of the load current and voltage
  - **No cross-coupling** between current and voltage harmonic components

$$\begin{aligned}
 S &\approx \sum_{k=1}^{k_m} V_k I_k && \text{linear relationship} \\
 &= \sum_{k=1}^{k_m} y_{kk} V_k^2, && \text{between current and} \\
 &&& \text{voltage harmonics} \\
 &&& I_k = y_{kk} V_k
 \end{aligned}$$

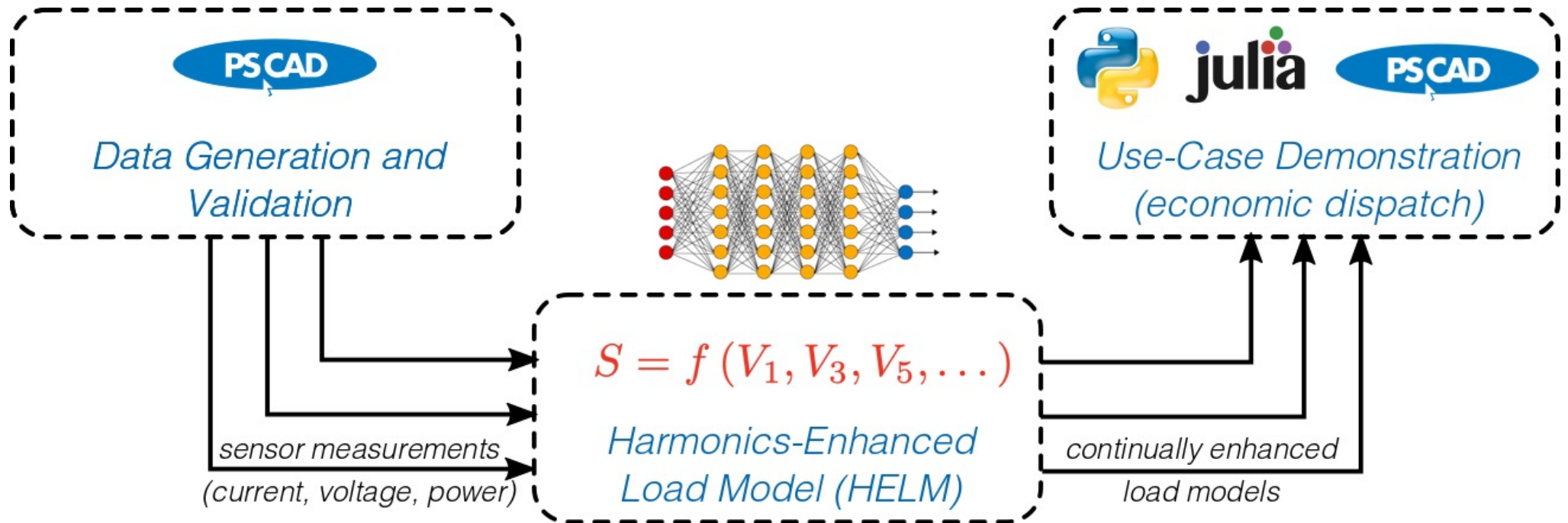
# What We Cover Today

- Harmonic Load Models
- **The HELM approach**
  - Overall framework
  - HELM modeling algorithms
  - Setup for data generation
- Current results and plan

# Proposed HELM Framework

*Electromagnetic modeling of PE and other resources, and synthetic data generation*

*Demonstrate the impact of model enhanced model on operations. Example: transformer overheating, optimal dispatch*



*Use time-series (point-on-wave) measurements to develop the harmonic-enhanced models, using optimization and machine learning (ML) methods*

# Harmonic-Enhanced Modeling: Frequency Coupling Matrix & Linear Regression

- **Frequency Coupling Matrix (FCM)**

- Allows **cross-coupling between load current and voltage**, via a linear relationship
- Also generalized Norton model, cross admittance matrix, harmonic admittance matrix
- **Linear regression (least squares) algorithm** to identify the FCM from data

$$\begin{aligned}
 S &\approx \sum_{k=1}^{k_m} V_k I_k \\
 &= \sum_{k=1}^{k_m} \sum_{l=1}^{k_m} y_{kl} V_k V_l
 \end{aligned}
 \quad
 \begin{bmatrix} I_1 \\ I_3 \\ \vdots \\ I_{k_m} \end{bmatrix}
 =
 \underbrace{\begin{bmatrix} y_{11} & y_{13} & \cdots & y_{1,k_m} \\ y_{31} & y_{33} & \cdots & y_{3,k_m} \\ \vdots & \vdots & \ddots & \vdots \\ y_{k_m,1} & y_{k_m,3} & \cdots & y_{k_m,k_m} \end{bmatrix}}_{\text{FCM}}
 \begin{bmatrix} V_1 \\ V_3 \\ \vdots \\ V_{k_m} \end{bmatrix}$$

**Drawback: assumes linearity in relationship between harmonics**

# Harmonic-Enhanced Modeling: Nonlinear Regression via Neural Network

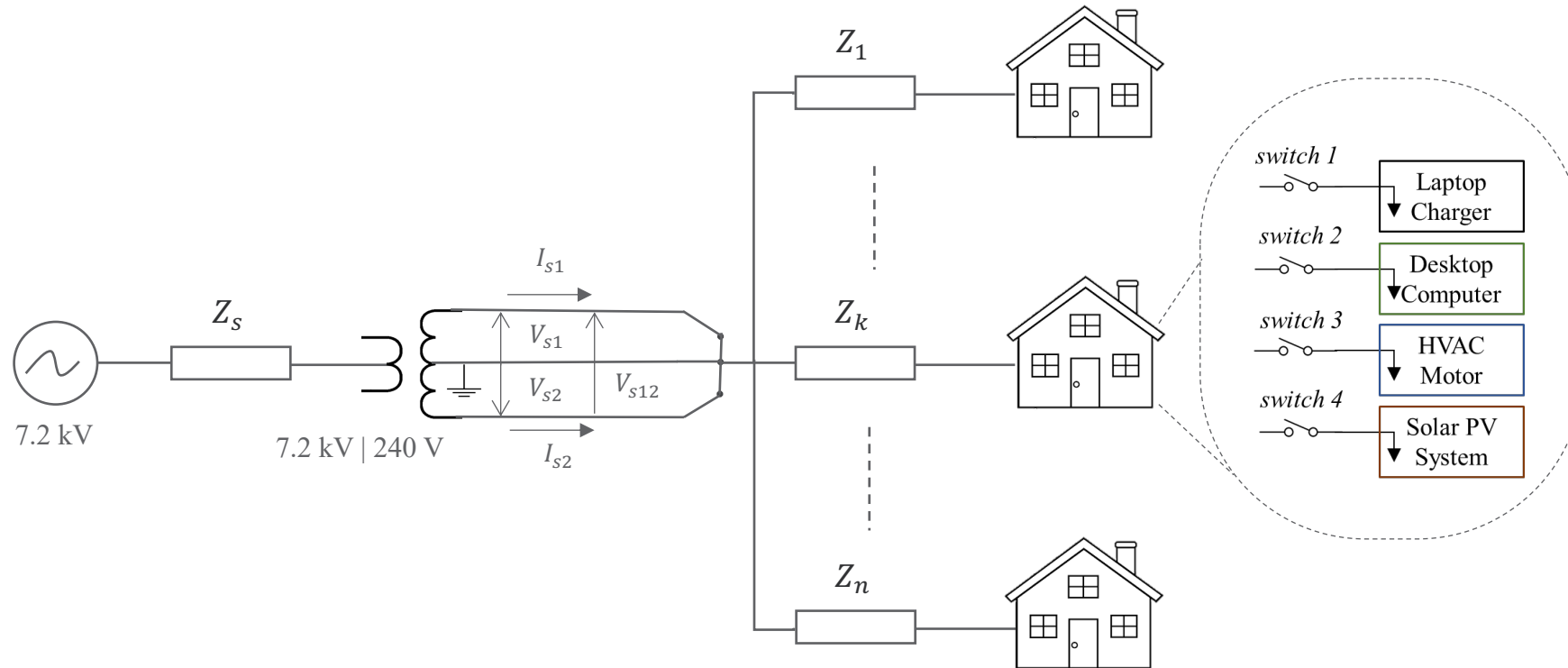
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  - **Linear regression (least squares) algorithm** to identify the FCM from data
- **Nonlinear Coupling Model**
  - Allows **cross-coupling between load current and voltage**, via a **nonlinear** relationship
  - **Feedforward neural networks** to perform nonlinear regression analysis

$$\begin{bmatrix} I_1 \\ I_3 \\ \vdots \\ I_{k_m} \end{bmatrix} = \begin{bmatrix} f_1(V_1, V_3, \dots, V_{k_m}) \\ f_3(V_1, V_3, \dots, V_{k_m}) \\ \vdots \\ f_{k_m}(V_1, V_3, \dots, V_{k_m}) \end{bmatrix}$$



***More generalized model, but possibly higher data requirement***

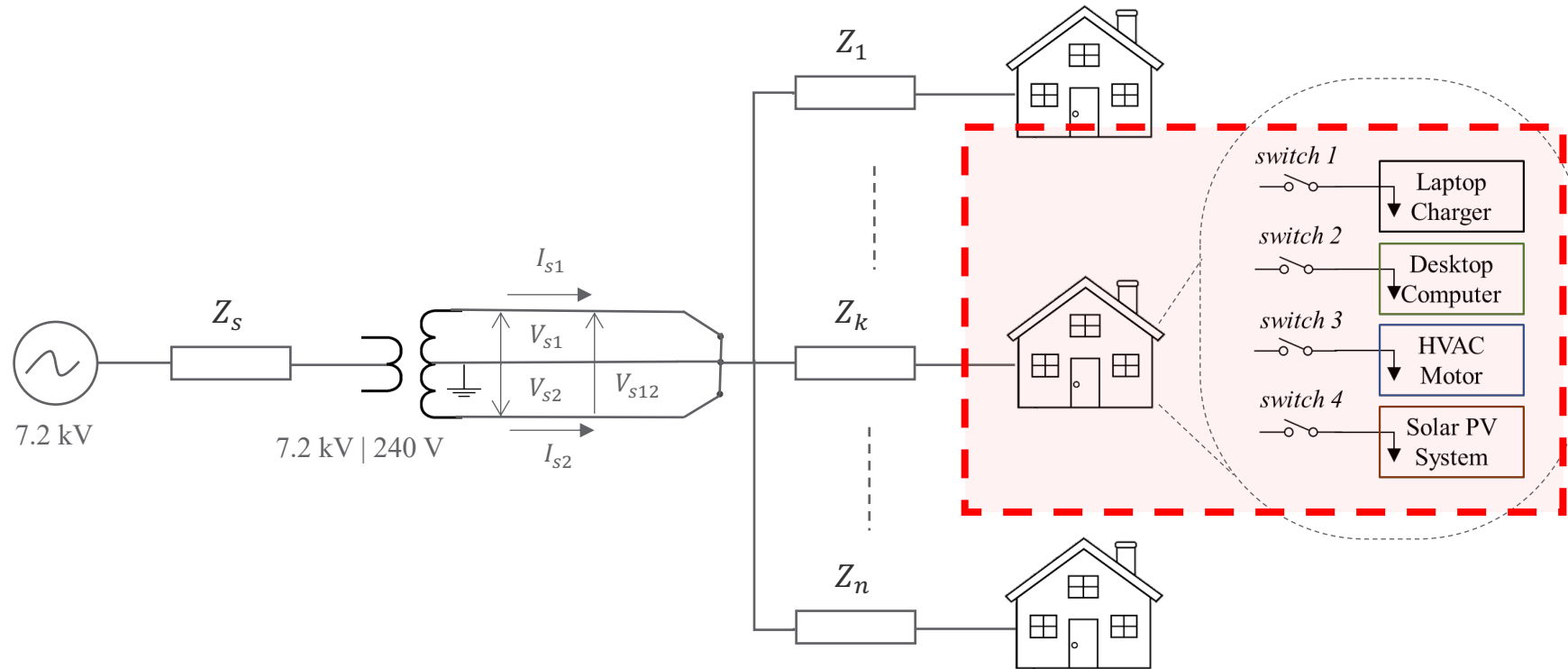
# Synthetic Data Generation



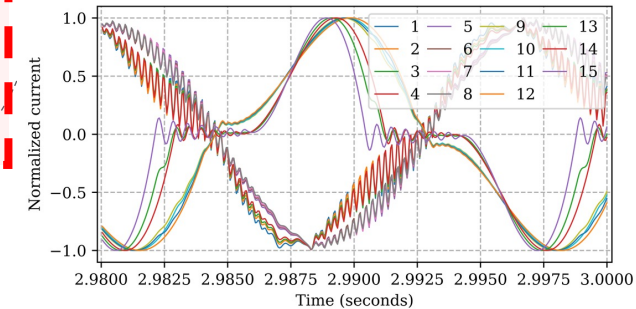
- Address dearth of feeder-wide data in harmonic studies
- Capture the impact and interactions of emerging PE load

- PSCAD-based simulation models for feeder-wide interaction between multiple houses with PE and nonlinear loads: laptop, desktop, HVAC, PV inverter
- Generate synthetic harmonics data by varying the terminal voltage THD

# Synthetic Data Generation



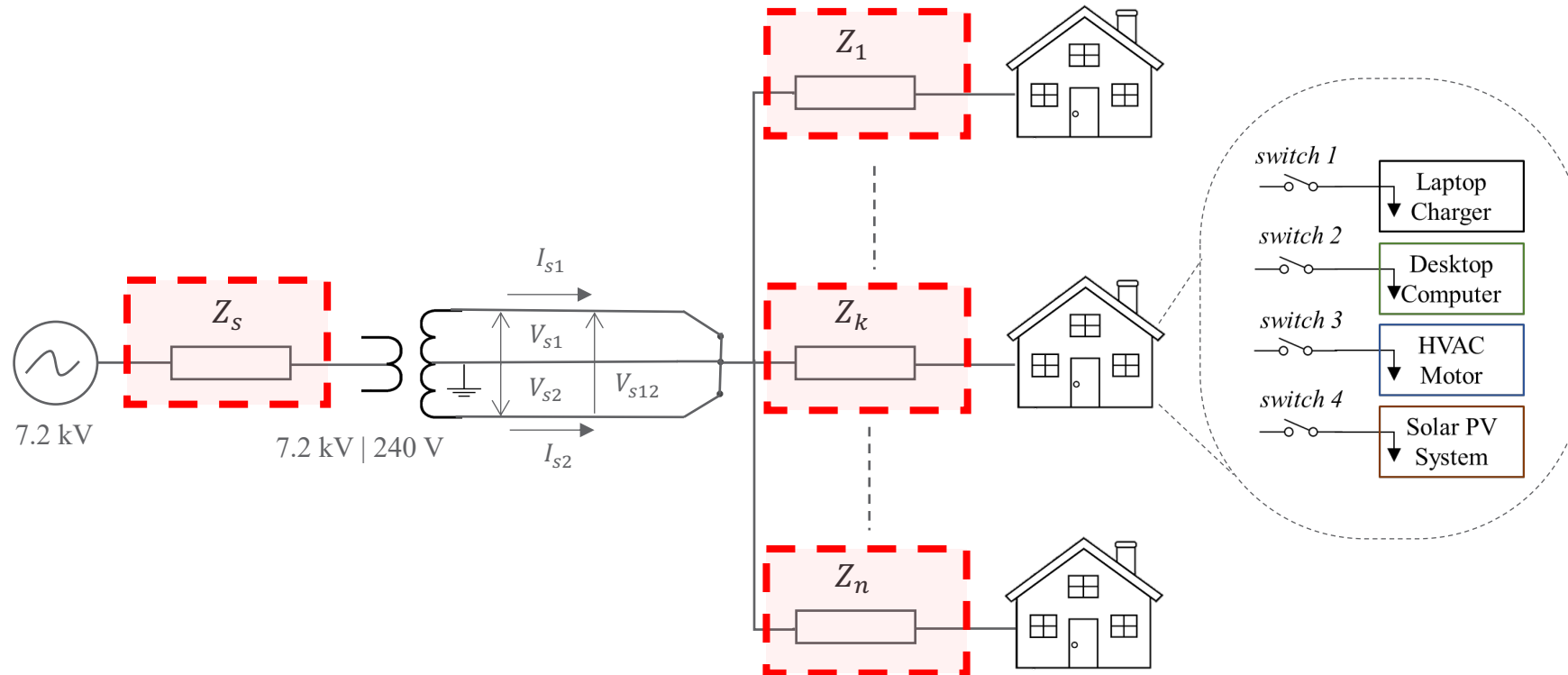
Switches used to create various load compositions and harmonic patterns in each house



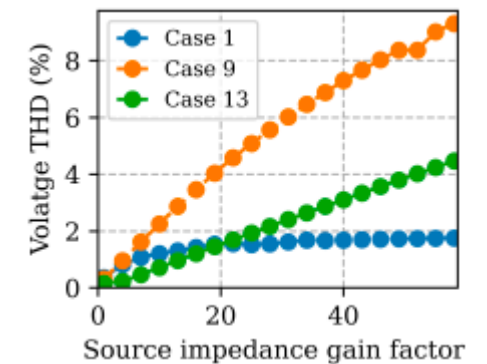
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# Synthetic Data Generation



Vary the source impedance for different voltage THD at house terminals (mimic feeder-wide impact)



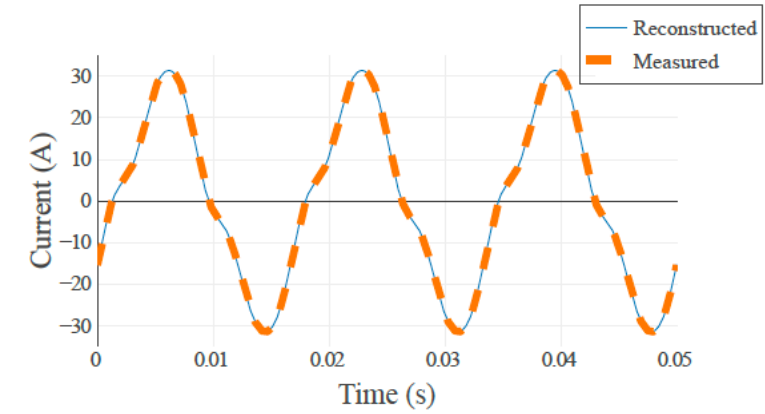
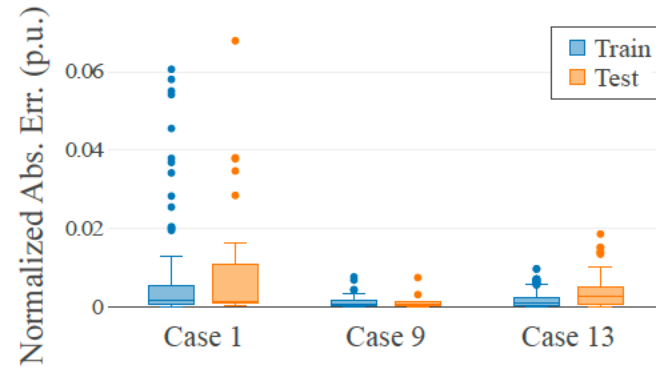
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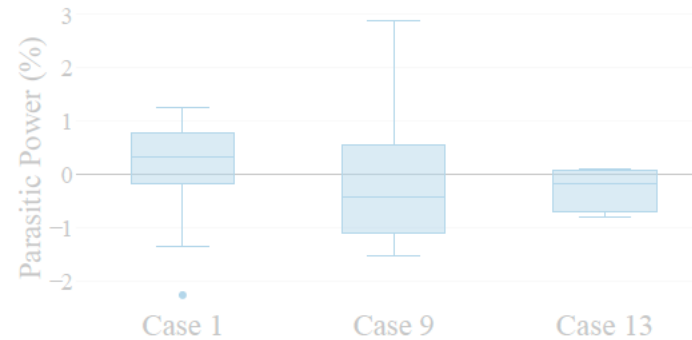
- Harmonic Load Models
- The HELM approach
- **Current results and plan**
  - Validation results
  - Ongoing work

# Results: Accuracy of FCM (linear regression)

- Accuracy of the identified harmonic load models
- Low reconstruction loss (largely <1%) across all cases
- Reconstructed current signal closely matches observation



- Contribution of non-fundamental harmonic components to power
- Parasitic power observed to be 2-3% of the ZIP load estimate (i.e., the fundamental power)

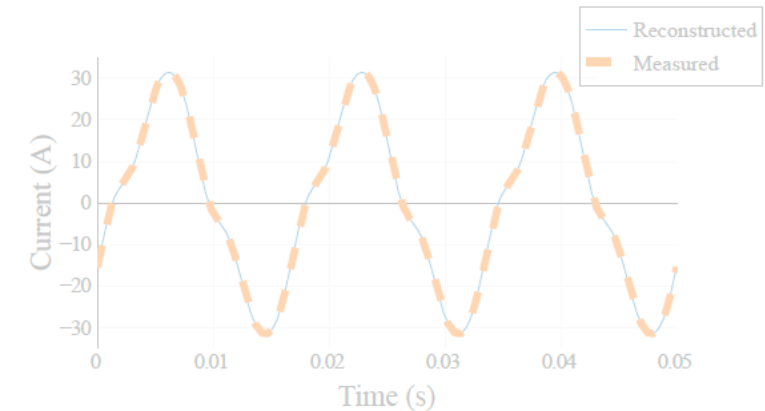
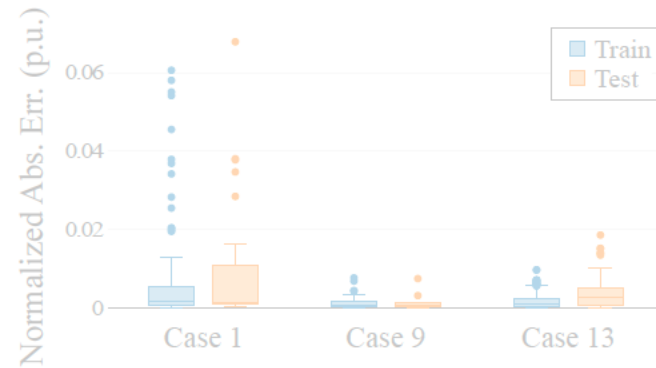


*Parasite power is the cumulative contributions to power from all non-fundamental harmonics*

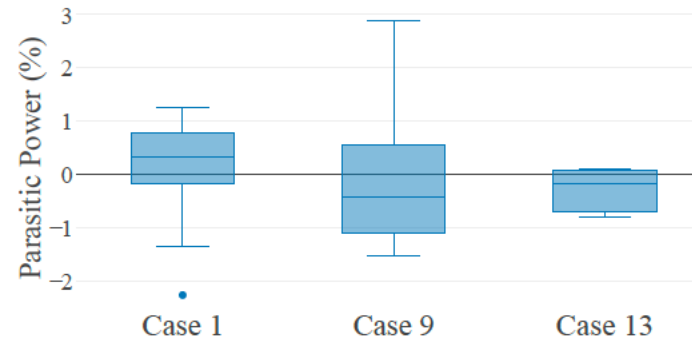
***Accurate estimate of harmonic load model. Improvement over ZIP.***

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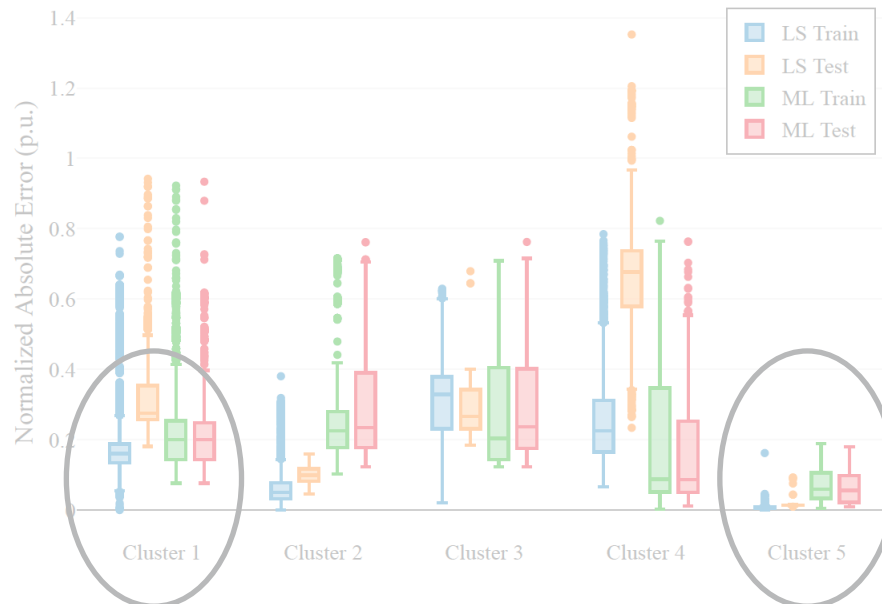


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# Results: Real data and neural network model

- Real data from MIT REDD 2011 study used for validating neural net models
  - Single house measurement over 1 month used for validation
  - Different load compositions (clusters) identified based on harmonic patterns
  - Comparing least squares (LS) and machine learning (ML) methods for accuracy

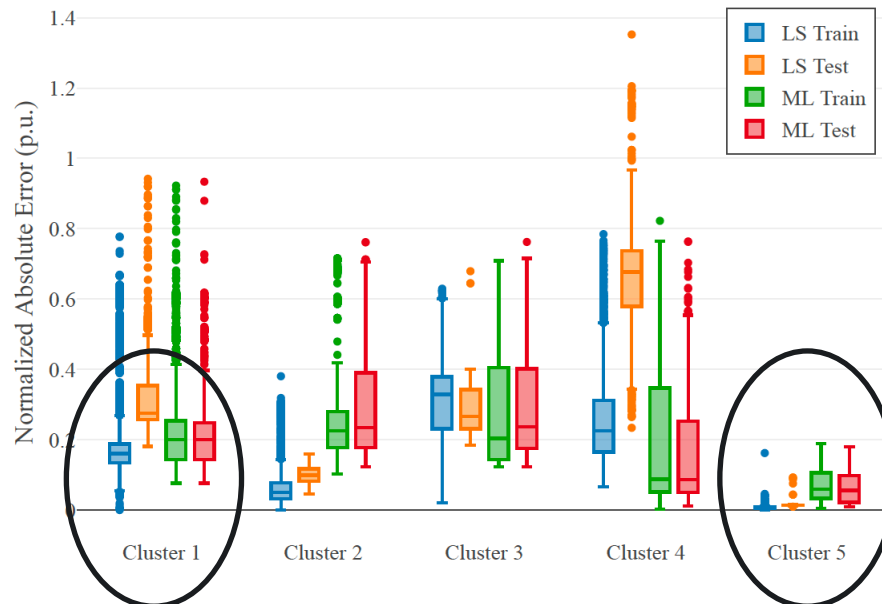


- *ML-based nonlinear regression model requires high data*
- *ML (nonlinear) outperforms LS (linear) in load composition 1 with most data-points*
- *LS outperforms ML in load composition 5 with the fewest data-points*

***Nonlinear model outperforms linear FCM under high data environment***

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# Continuing directions and outreach

- **Continual update** of load models
  - Methods such as **recursive least squares** and **transfer learning** for online updates
- Studying the **feeder-level impact** of harmonics
  - Eddy (harmonic) current losses causing **overheated transformers**
  - Inaccurate load models leading to **sub-optimal dispatch** of DERs
  - **Extension to T+D** studies with aggregated harmonic models
- **Real-world experimental data** collections and validation
  - Ongoing discussions to collect house-level harmonic measurements at varying voltage
- **Publication (ISGT 2022):**
  - Singhal, Wang, Reiman, Liu, Hammerstrom, and Kundu. “Harmonic Modeling, Data Generation, and Analysis of Power Electronics-Interfaced Residential Loads”.



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**Thank you**

**Questions?**

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